

NAG Quant Seminar / Finance Focus Event

Latest releases and news

John Holden

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nag[®]

Experts in numerical algorithms
and HPC services

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CQF

The NAG Library is now at Mark 23

Now available as:

- The NAG Fortran Library
- The NAG Library for SMP & Multicore
- The NAG C Library
- The NAG Toolbox for MATLAB

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- The NAG C Library *1st implementations available*
- The NAG Toolbox for MATLAB

1st implementations became available this week!

The NAG Library Contents

- Root Finding
- Summation of Series
- Quadrature
- Ordinary Differential Equations
- Partial Differential Equations
- Numerical Differentiation
- Integral Equations
- Mesh Generation
- Interpolation
- Curve and Surface Fitting
- optimisation
- Approximations of Special Functions
- Dense Linear Algebra
- Sparse Linear Algebra
- Correlation & Regression Analysis
- Multivariate Methods
- Analysis of Variance
- Random Number Generators
- Univariate Estimation
- Nonparametric Statistics
- Smoothing in Statistics
- Contingency Table Analysis
- Survival Analysis
- Time Series Analysis
- Operations Research

The NAG Toolbox and NAG C Library

Senior quant from Tier 1 Investment Bank

“We deploy production code in C++ embedding NAG C Library functions wherever we can, but often prototype new models in MATLAB before writing our C++ code. Having the same NAG algorithms in MATLAB via the NAG Toolbox for MATLAB is a real win for us”

NAG Toolbox: Ease of use improvements

- **Function Handles**

- In previous versions of the NAG Toolbox for MATLAB, users had to provide some parameters as m-files. While this functionality is still supported, users may also provide parameters as function handles.

- **Better Exception handling**

- **Integer Utility introduced**

- Making it easier to write portable code between 32 & 64 bit platforms

- **Improved example programs and long names**

NAG Library : *new* Mark 23

Mark 23 has new functions in many areas including...

■ Wavelet Transforms

- One dimensional continuous transforms
- Two dimensional discrete single level and multi-level transforms

■ ODE's

- BVP solution through Chebyshev pseudo-spectral method

■ Matrix Operations

- Matrix exponentials
- Functions of real symmetric and Hermitian matrices
- Sparse matrix functions
- LAPACK 3.2 Cholesky solvers and factorizations, and many other LAPACK driver functions

■ Interpolation

- Modified Shepard's method in 4D/5D

■ New vector functions* (in G01 and S)

■ optimisation

- Multi-start optimisation*
- Minimization by quadratic approximation (BOBYQA)
- Stochastic global optimisation using PSO

■ RNG's

- Generators of multivariate copulas
- Skip-ahead for Mersenne Twister
- L'Ecuyer MRG32K3a generator

■ Statistics

- Quantiles of streamed data, bivariate Student's t, and two probability density functions
- Nearest correlation matrices
- Quantile regression
- Peirce Outlier detection
- Anderson–Darling goodness-of-fit

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Focus on new routines in Mark 23

- Slides derived from <http://www.nag.com/numeric/cl/newarticles23>

Focus on new routines at Mark 23 (1)

■ Matrix functions

- exponential, principal logarithm, sine, cosine, sinh, cosh
 - further marks will include square roots, non-integer powers...
- used in the solution of differential equations

$$\frac{d\mathbf{y}}{dt} = A\mathbf{y} \Rightarrow \mathbf{y} = \mathbf{y}_0 e^{At}$$

- used in Markov chains in finance
 - given the transition probability matrix, often want its p-th root
- used in graph theory
 - given the network matrix, its exponential measures connectedness

Focus on new routines at Mark 23 (2)

Global optimisation

■ Multilevel Coordinate Search method

added at Mark 22

- Handles simple bound constraints only
- Derivatives are not required

■ Multiple-start algorithms for optimisation

- run local optimizer from several different points
 - users have asked for a list of all local minima – not just the global
 - useful when other criteria exist for an acceptable solution
- alternative to more complicated global optimisation methods

Focus on new routines at Mark 23 (3)

- Particle Swarm optimisation - some might say *“Method of last resort!”*
 - The routines search for a global minimum using a variant of the particle swarm heuristic.
 - This involves the initialization of a ‘swarm’ of particles in hyperspace, which are advected through the domain using a velocity dependent upon ‘inertia’, ‘cognitive memory’ and ‘global memory’.
 - These routines are most effectively used when multiple cores are available for computation.

Focus on new routines at Mark 23 (4)

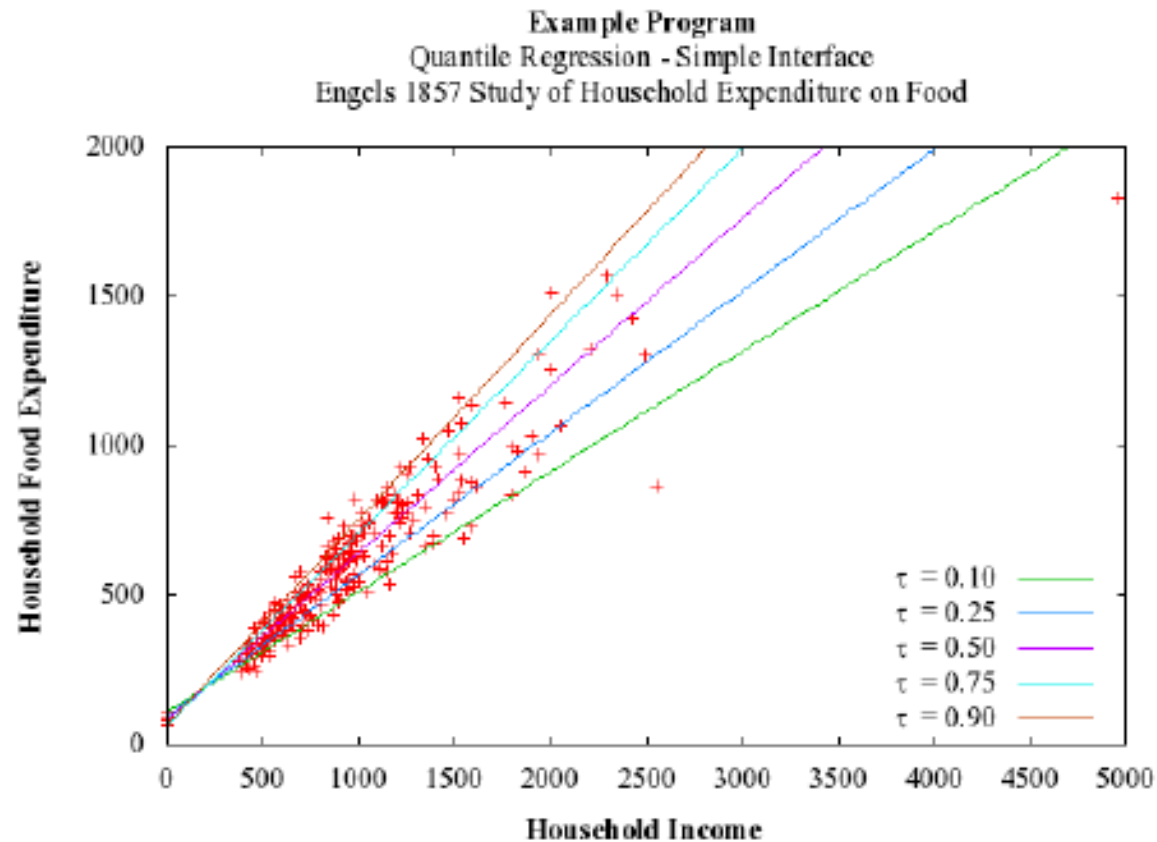
- **Bound optimisation BY Quadratic Approximation**
 - robust, easy-to-use minimization routine
 - minimizes objective function subject to bound constraints
 - uses quadratic approximation and trust regions
 - doesn't require derivatives
 - useful in inverse problems – e.g. trying to infer material properties by matching simulation output to experimental measurement
 - Example: distribute 50 points equally on a sphere
 - BOBYQA : 4633 evaluations
 - Nelder-Mead simplex solver (also in NAG Library) : 16757 evaluations

Focus on new routines at Mark 23 (5)

■ Quantile regression

- models quantile of response variable
 - *cf.* least-squares regression, which models the mean
- allows for more comprehensive data analysis
 - potentially more insight into the data and underlying relationships
 - less sensitive to large outlying distributions
- used in, e.g., ecology
 - to discover more useful predictive relationships between variables
 - when there is only a weak relationship between means

Quantile regression example



Koenker R (2005) *Quantile Regression* Econometric Society Monographs, Cambridge University Press, New York

Focus on new routines at Mark 23 (6)

- Improvements to nearest correlation matrix
 - correlation matrix is used to construct sensible portfolios
 - gives correlation between stocks in portfolio
 - must be *positive semidefinite*
 - sometimes isn't – e.g. due to missing values
 - routine for nearest correlation matrix added to Mark 22
 - “closest approximation” to input (non-semidefinite) matrix
 - Mark 23 enhancements allow for use of
 - weighted norm
 - factor structure
 - incorporates more information about problem to be solved

Focus on new routines at Mark 23 (7)

Sampling = randomly selecting one or more observations or records from a particular dataset.

- **Sampling with unequal weights**
 - selecting records from a dataset
 - with / without replacement, with equal / unequal weights
 - without replacement, with unequal weights new in CL23
- **Sampling used widely**
 - selecting subjects for study in controlled experiment
 - converting from a continuous signal to a discrete one
 - re-using parts of sound recordings

Focus on new routines at Mark 23 (8)

- **Better Mersenne Twister Random Number Generator**
 - Mersenne Twister has very long period
 - also fast implementation and good statistical properties
 - Want to use it to create multiple streams
 - for parallel applications
 - Recommended method is skip-ahead
 - sequence is partitioned into non-overlapping streams
 - Now possible in Mark 23
 - generate multiple streams of huge numbers of values with no overlap
- **New routine for L'Ecuyer MRG32k3a RNG, as well**

COMING SOON.....

NAG and Java

Currently we steer the user to write their own wrappers and provide a few examples.

- Use JNI library to wrap calls to NAG routines
 - in either C Library or Fortran Library
 - Technical report with detailed examples available
 - online at www.nag.com
 - Wrappers for specific routines available from NAG
 - on request

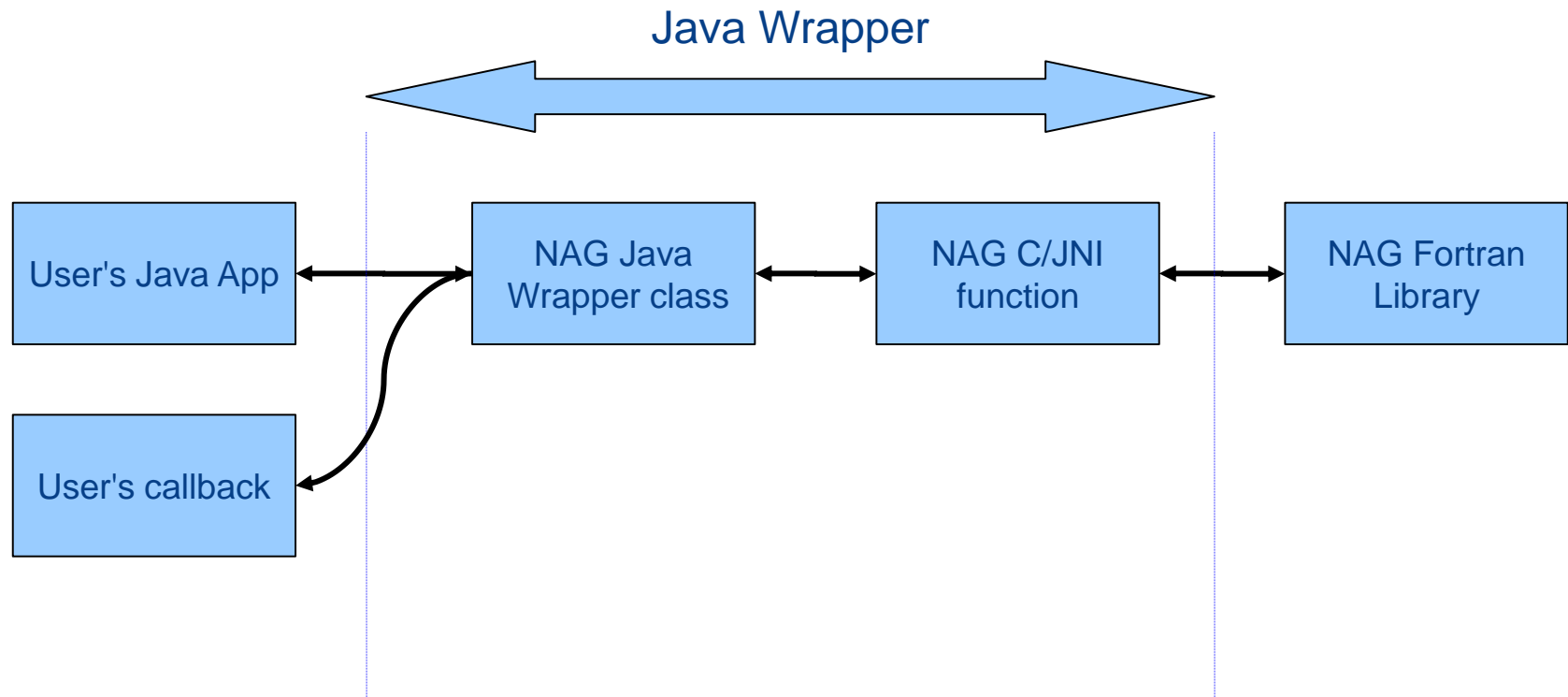
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For some of you this is NOT enough!

So coming soon.... The NAG Library *for Java*



Inside the wrapper

Java wrapper class

```
1 package com.nag.routines;
2
3 import ...
4
5 public class S17ACJ extends Routine{
6
7
8     private double X;
9     private int IFAIL;
10
11
12     public double getX(){
13         return this.X;
14     }
15     public void setX(double X){
16         this.X=X;
17     }
18     public int getIFAIL(){
19         return this.IFAIL;
20     }
21     public void setIFAIL(int IFAIL){
22         this.IFAIL=IFAIL;
23     }
24
25     public S17ACJ( double X, int IFAIL){
26         /*Initialising arguments*/
27         this.X = X;
28         this.IFAIL = IFAIL;
29     }
30
31     public double eval(){
32         Routine.ExtendedBuffer buff = new Routine.ExtendedBuffer(8 +4 ,2);
33
34         buff.put(X);
35         buff.put(IFAIL);
36         Routine.ExtendedBuffer resultBuff = new Routine.ExtendedBuffer(8,1);
37         byte[] result = resultBuff.getValues();
38         this.S17ACF(buff.getIndexes(),buff.getValues(),result);
39
40         //POST TREATMENT
41         buff.rewind();
42         this.X = buff.get(X);
43         this.IFAIL = buff.get(IFAIL);
44         double res = 0.0;
45         res = resultBuff.get(res);
46         return res;
47     }
48     public double eval( double X, int IFAIL){
49
50         this.X = X;
51         this.IFAIL = IFAIL;
52         return this.eval();
53     }
54
55     private native void S17ACF(int[] indexes, byte[] values, byte[] result);
56
```

C/JNI function

```
1 //##### INCLUDES SECTION #####
2 #include <naglibutilities.h>
3 #include <com_nag_routines_S17ACJ.h>
4 #include <string.h>
5 //##### END INCLUDES SECTION #####
6
7 //##### EXTERN SECTION #####
8 extern double s17acf (jbyte *arg_0 ,jbyte *arg_1 );
9 //##### END EXTERN SECTION #####
10
11 //##### GLOBAL VARIABLES SECTION #####
12 //NO GLOBAL VARS REQUIRED
13 //##### END GLOBAL VARIABLES SECTION #####
14
15 //##### CALLBACKS SECTION #####
16 //NO CALLBACK FOR THIS ROUTINE
17 //##### END CALLBACKS SECTION #####
18
19 //##### JNI FUNCTION SECTION #####
20 JNIEXPORT void JNICALL Java_com_nag_routines_S17ACJ_S17ACF(JNIEnv *env, jobject obj,
21     jintArray indexes, jbyteArray values, jbyteArray result){
22     jint *C_indexes = getIntArrayFromJava(env,indexes);
23     jbyte *C_values = getByteArrayFromJava(env,values);
24     jbyte *C_result = getByteArrayFromJava(env,result);
25
26
27     double res = s17acf_(
28         &C_values[C_indexes[0]],
29         &C_values[C_indexes[1]]);
30
31     memcpy((void*)&C_result[0],(void*)&res,8);
32     setByteArrayToJava(env,values,C_values);
33     setIntArrayToJava(env,indexes,C_indexes);
34     setByteArrayToJava(env,result,C_result);
35 }
36 //##### END JNI FUNCTION SECTION #####
37
38
```

Calling the NAG Library *for Java*

```
import com.nag.routines.e04.E04GB;

[...]
```

```
public static main(String[] args){
    [...]
    LSQFUN lsqfun = new LSQFUN();
    [...]
    E04GB e04gb = new E04GB(m, n, lsqlin, lsqfun, lsqmon, iprint, maxcal, eta, xtoll,
                          stepmx, x, fsumq, fvec, fjac, ldfjac, s, v, ldv, niter,
                          nf, iw, liw, w, lw, ifail);

    [...]
    e04gb.eval();
    ifail = e04gb.getIFAIL();
    [...]
}

private static class LSQLIN implements E04GBJ.E04GBJ_LSQLIN {
    [...]
    public void eval(int SELCT) {
        this.SELCT = SELCT;
        E04HEV e04hev = new E04HEV(SELCT);
        e04hev.eval();
        this.SELCT = e04hev.getLSQLIN_SELECT();
    }
}
```


Many-core & GPU

- Developed CUDA software for Monte Carlo
 - new work for a PDE Solver for Stochastic Local Volatility progressing well
- Collaboration with Intel on MIC architecture
- Considerable expertise for training and consulting in
 - OpenCL
 - CUDA
 - use of libraries such as MAGMA and PLASMA
 - with plans to integrate into the NAG Library

NAG Library Development Continues....

- **NAG Library for .NET**
 - Following the success of the first release a second release is scheduled for 2013
 - new functions will include optimisation, NCM,...
 - Updated documentation for usage with VS2012
- **Work already underway for Mark 24 of**
 - NAG Fortran, NAG C, NAG Toolbox for MATLAB,...
- **Algorithmic Differentiation (AD)**
 - As well as providing training and consultancy we will be implementing AD versions of existing NAG Library functions

Finally....

- Thank you and.....

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KEEP TELLING US WHAT YOU WANT